

Cosmic Radio Dipole

Overdispersed radio source counts and excess radio dipole detection

LOFAR Family Meeting 2025

Lukas Böhme

Cosmic Radio Dipole

ACCEPTED PAPER

Overdispersed radio source counts and excess radio dipole detection

Lukas Böhme, Dominik J. Schwarz, Prabhakar Tiwari, Morteza Pashapour-Ahmadabadi, Benedict Bahr-Kalus, Maciej Bilicki, Catherine L. Hale, Caroline S. Heneka, and Thilo M. Siewert

Phys. Rev. Lett. - **Accepted** 19 September, 2025

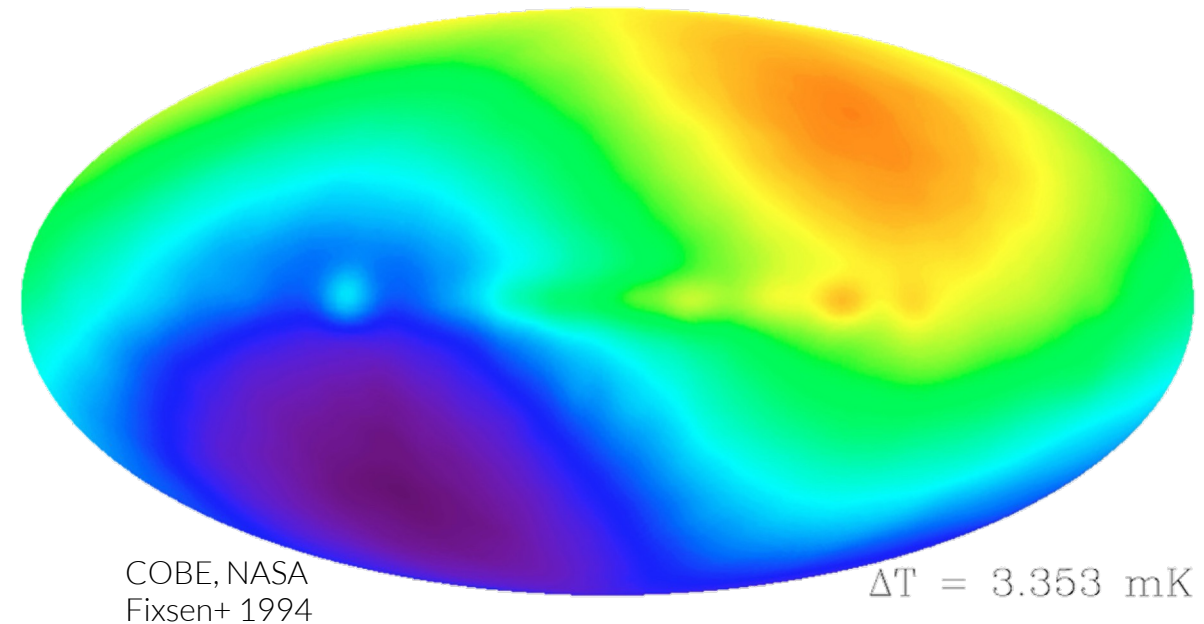
DOI: <https://doi.org/10.1103/6z32-3zf4>

[Export Citation](#)

Cosmic Microwave Background

- First noted in 1967/69 [1]
- Clear result: 1994 COBE [2]
- Assumption: Only due to motion of the Solar System in relation to CMB rest-frame
- On the order of 10^{-3}

$$v_{\text{CMB}} = 369.82 \pm 0.11 \text{ km s}^{-1} \quad [3]$$



[1] Partridge and Wilkinson, 1967

[2] Fixsen et al. 1994

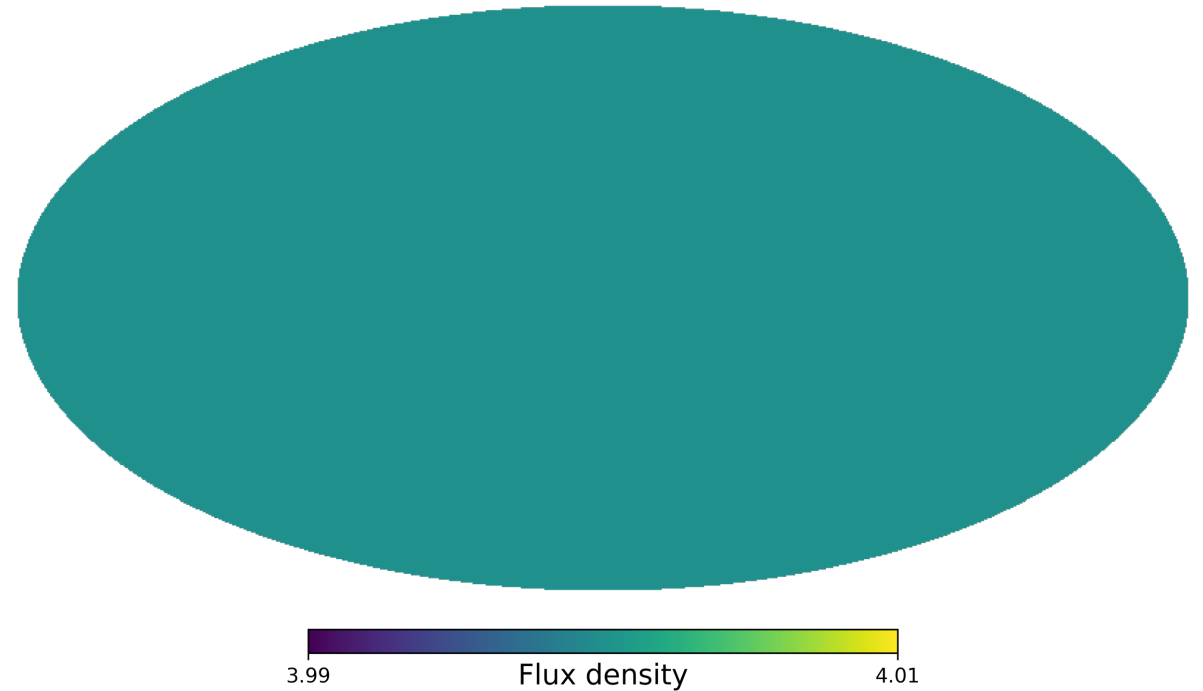
[3] Planck Collaboration 2020

Cosmic Radio Dipole

- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration

Cosmic Radio Dipole

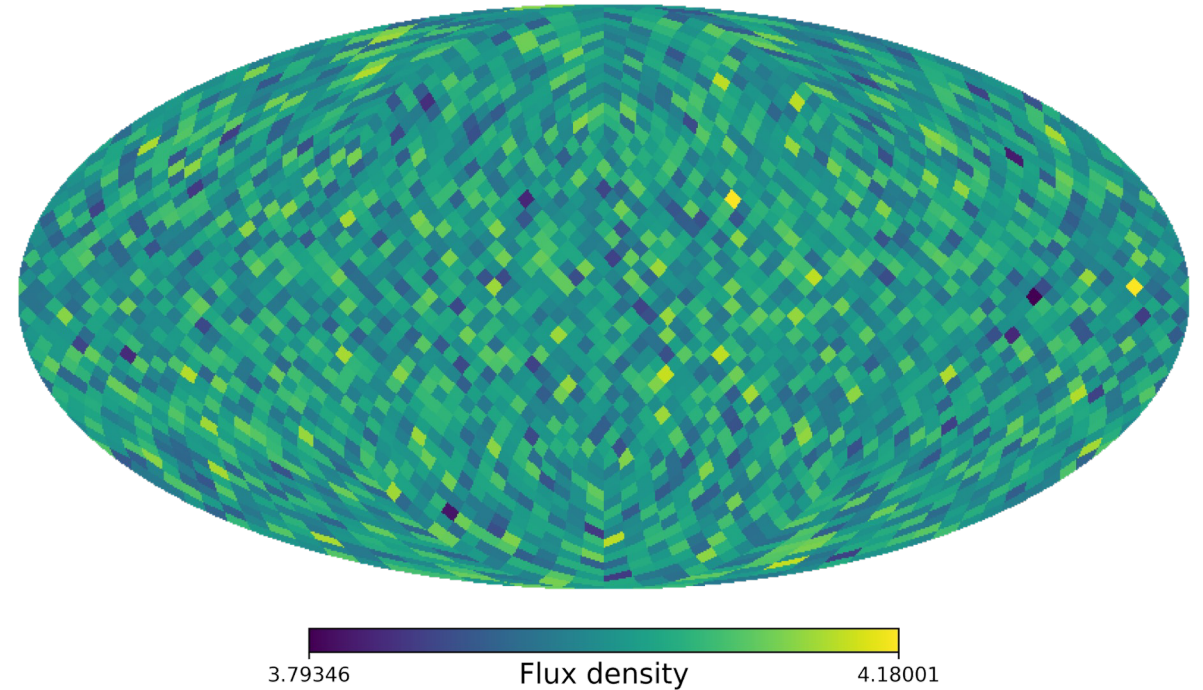
- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration



Each pixel $\triangleq$ 1 source at 4mJy

Cosmic Radio Dipole

- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration



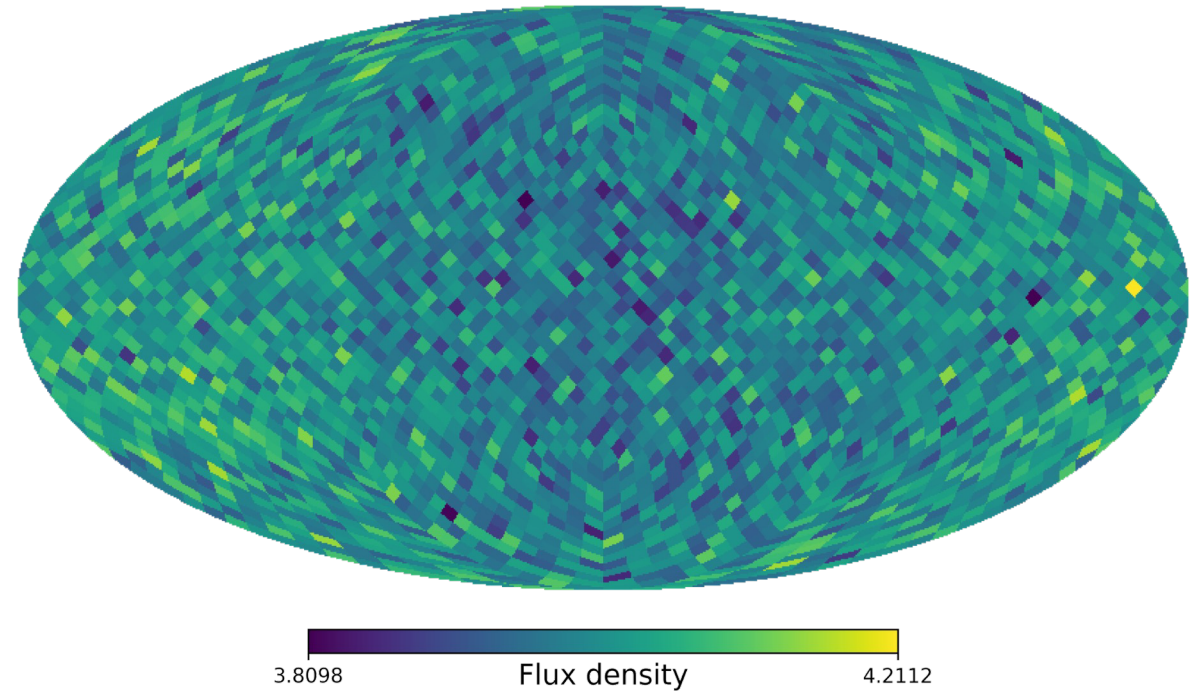
Each pixel $\triangleq$ 1 source at 4mJy + Noise

Cosmic Radio Dipole

- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration

Doppler shift

- Change in frequency
 - Change in flux density ($S \propto \nu^{-\alpha}$)



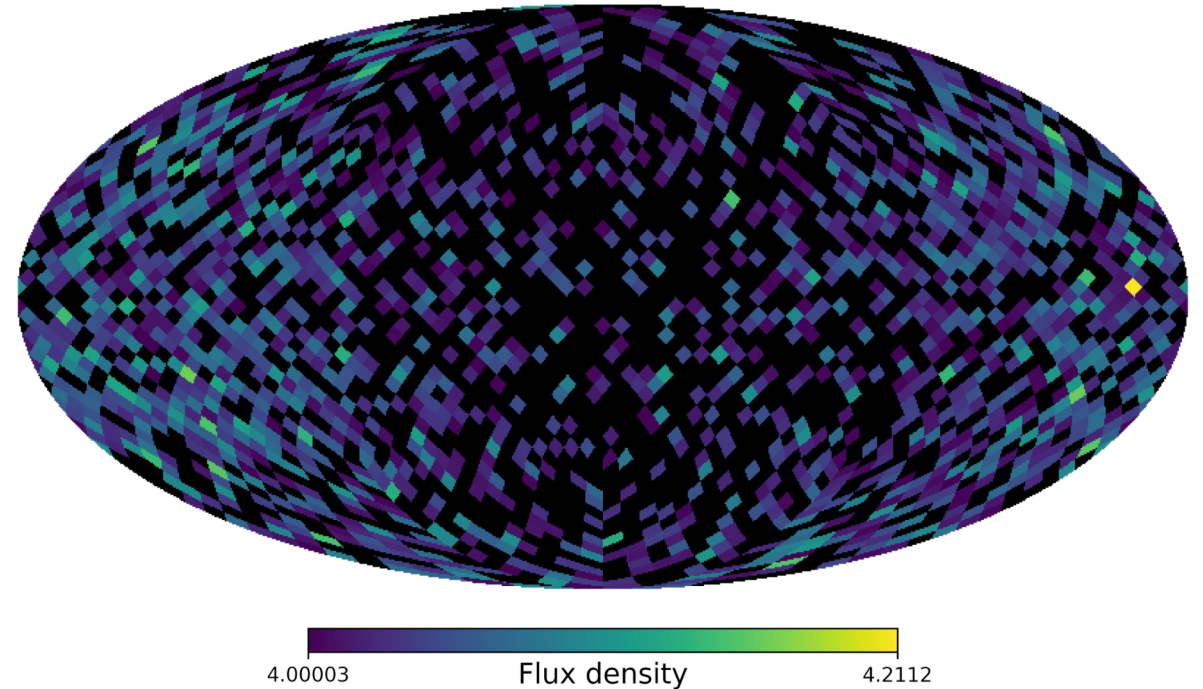
Each pixel $\triangleq$ 1 source at 4mJy + Noise
+ Doppler shift

Cosmic Radio Dipole

- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration

Doppler shift

- Change in frequency
 - Change in flux density ($S \propto \nu^{-\alpha}$)



Each pixel $\triangleq$ 1 source at 4mJy + Noise
+ Doppler shift
+ 4mJy flux cut

Cosmic Radio Dipole

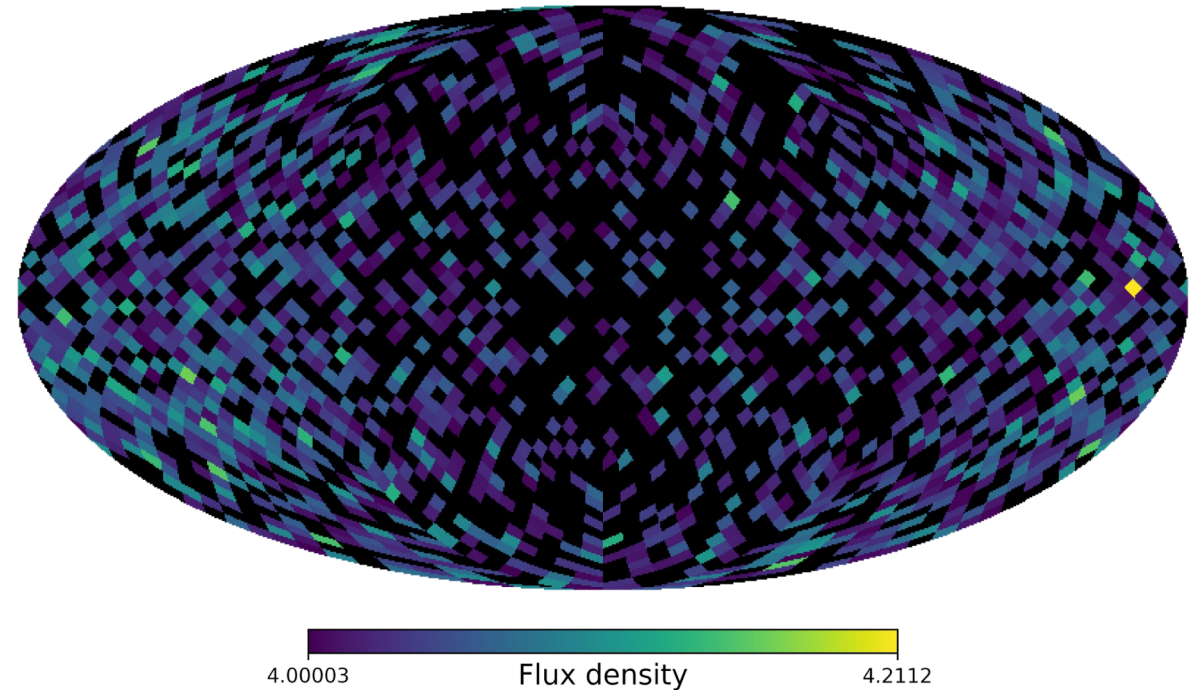
- $\bar{z} \approx 1$
- $d_{\text{radio}} = d_{\text{kin}} + d_{\text{cluster}}$
- d_{cluster} expected to be small (local)
- d_{kin} due to Doppler shift & Aberration

Doppler shift

- Change in frequency
 - Change in flux density ($S \propto \nu^{-\alpha}$)

Aberration

- Change of observed angle towards direction of motion („Clustering“)



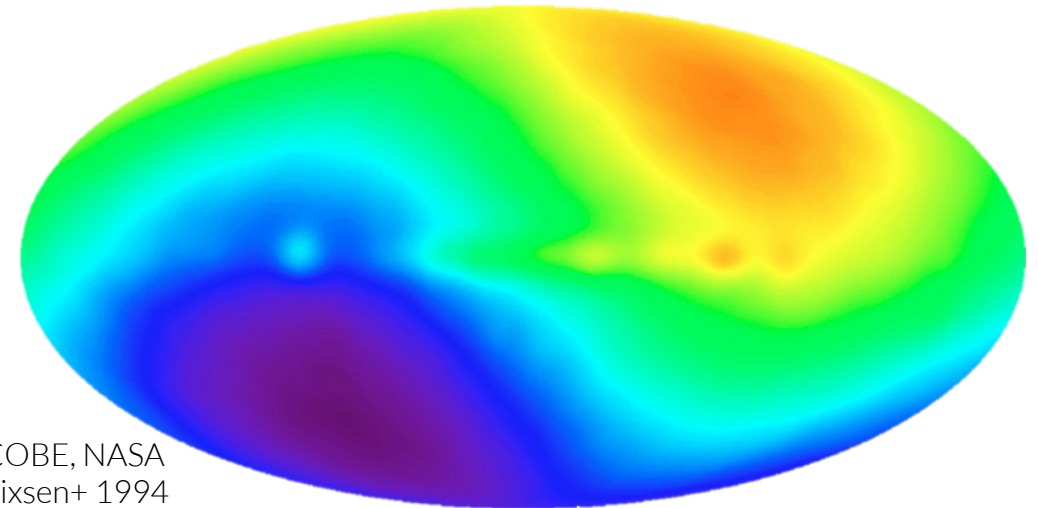
Each pixel $\triangleq$ 1 source at 4mJy + Noise
+ Doppler shift
+ 4mJy flux cut

Source Count Dipole

Counts-in-cell

↙

$$\left. \frac{dN}{d\Omega} \right|_{\text{obs}} = \left. \frac{dN}{d\Omega} \right|_{\text{rest}} (1 + d \cos \theta)$$



Source Count Dipole

Counts-in-cell

$$\frac{dN}{d\Omega}\bigg|_{\text{obs}} = \frac{dN}{d\Omega}\bigg|_{\text{rest}} (1 + d \cos \theta)$$

$\theta = \angle$ (Pixel, direction of motion)

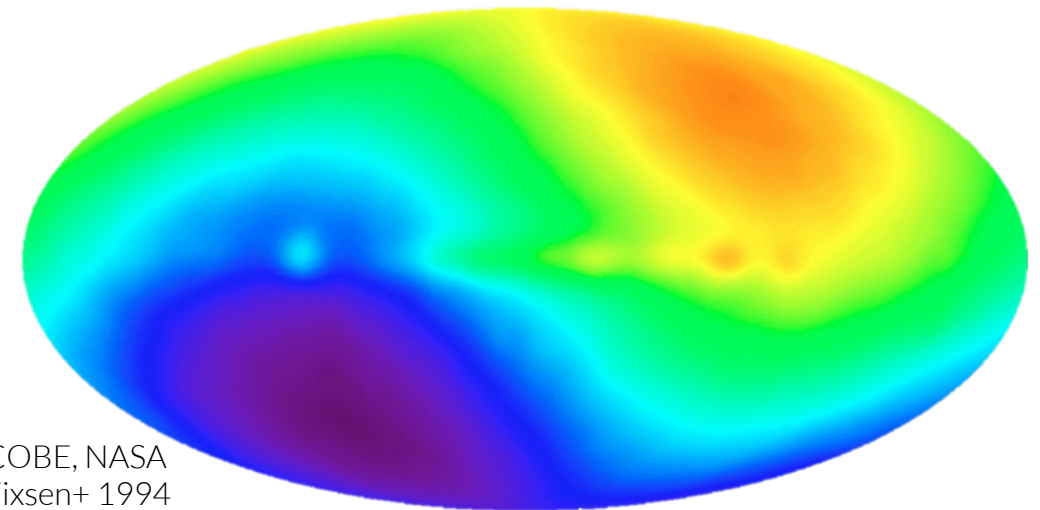
$$\left. \begin{array}{l} dN/d\Omega(> S) \propto S^{-x} \text{ Slope in source counts} \\ S \propto \nu^{-\alpha} \text{ Spectral index} \end{array} \right\} @S_{\min}$$

Radio survey dependent

$$d_{exp} = (2 + x(1 + \alpha)) \frac{v_{\text{CMB}}}{c} \approx 0.5 \times 10^{-2}$$

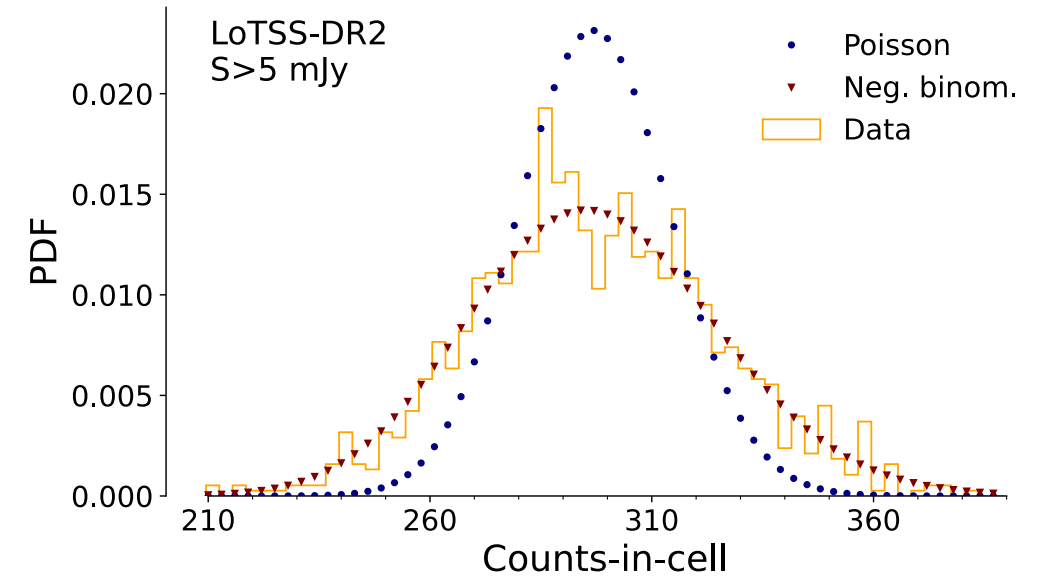
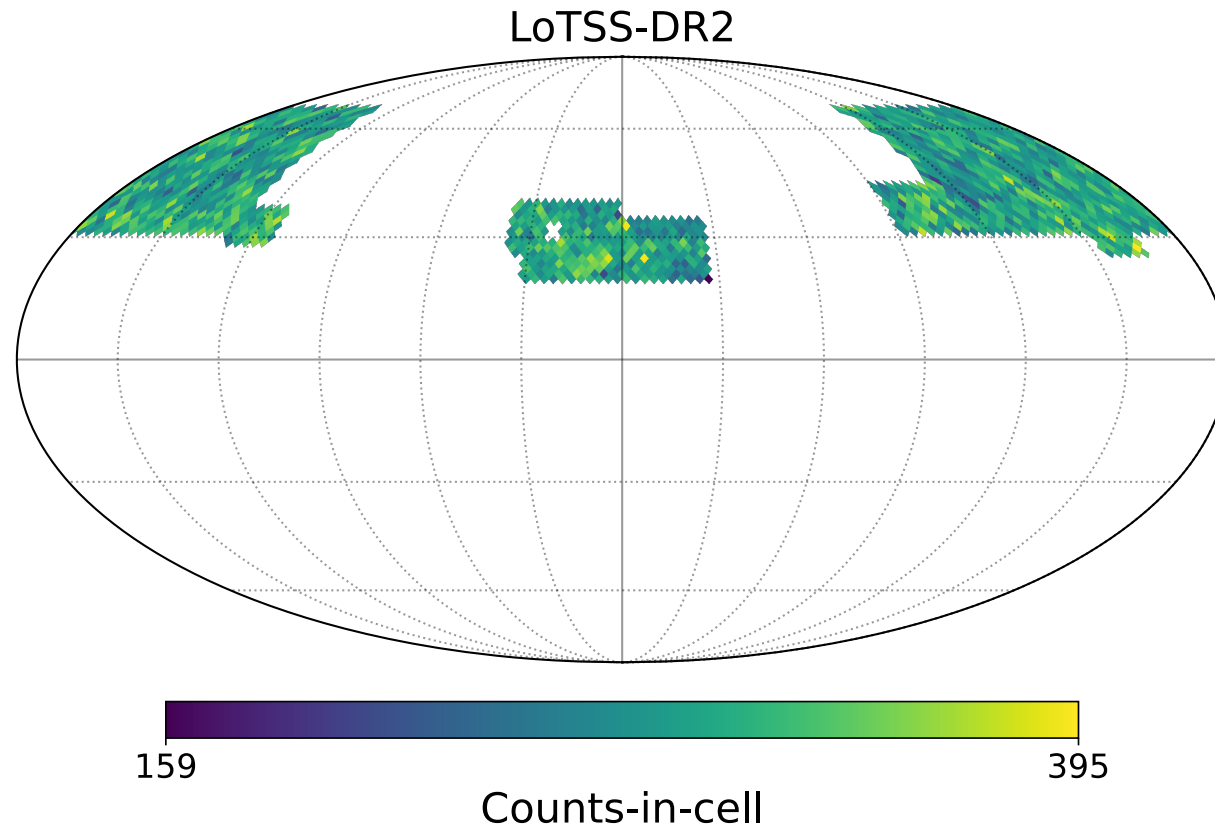
$\Rightarrow$ 0.5% effect at max and min

$$v_{\text{CMB}} = 369.82 \text{ km s}^{-1}$$



COBE, NASA
Fixsen+ 1994

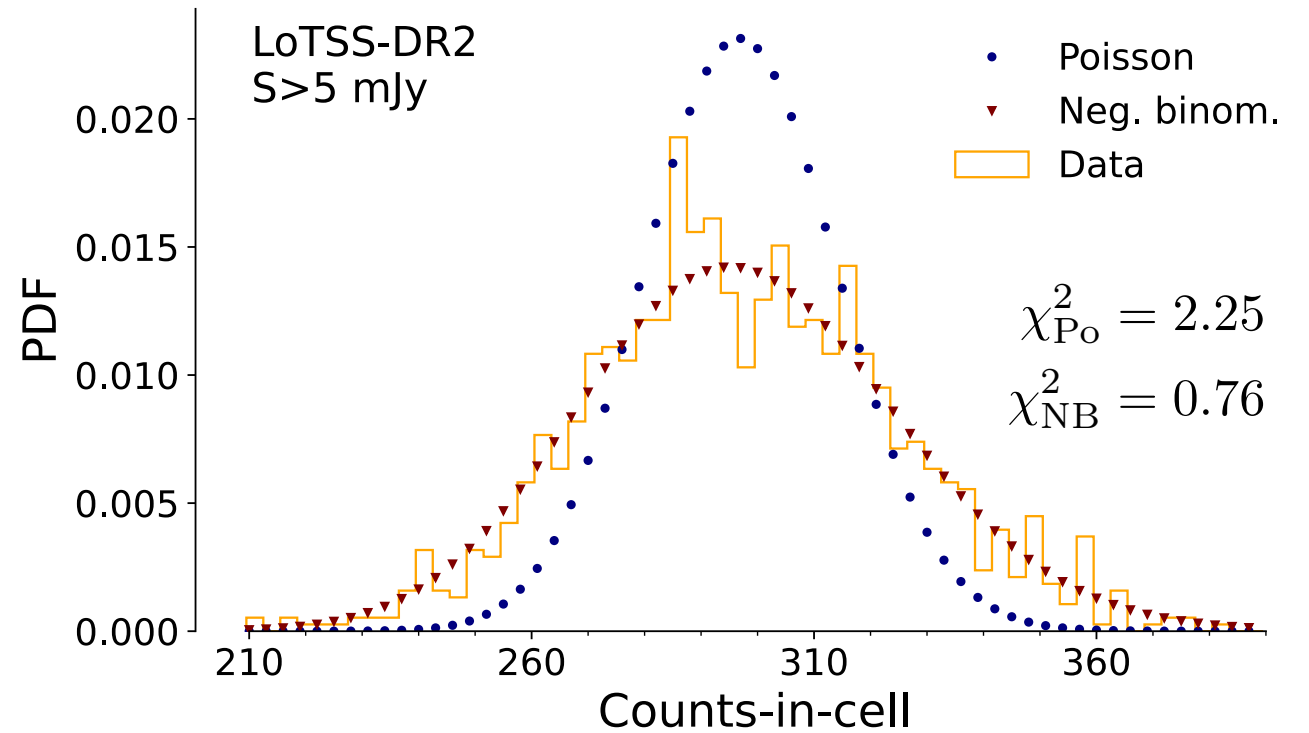
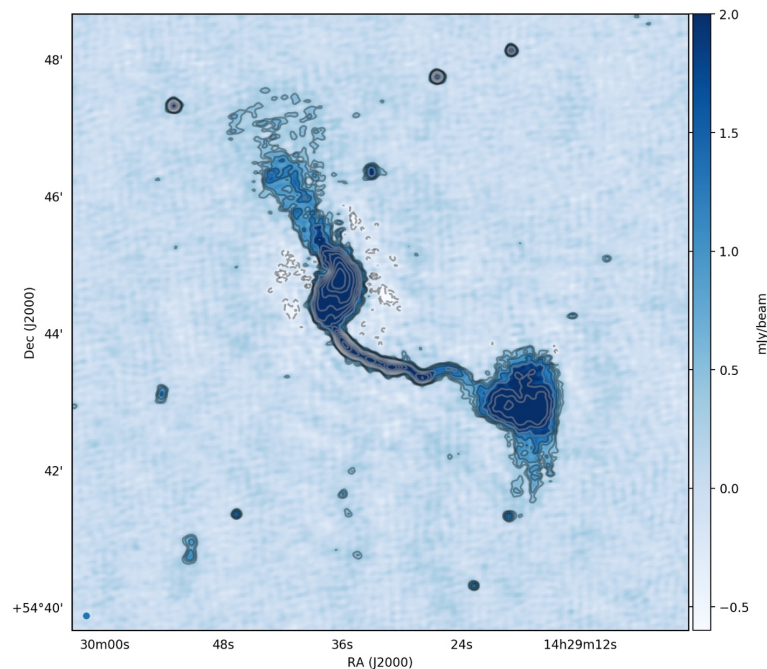
Counts-in-cell



Counts-in-cell

✗ Poisson distr. Point sources

✓ Negative binomial distribution



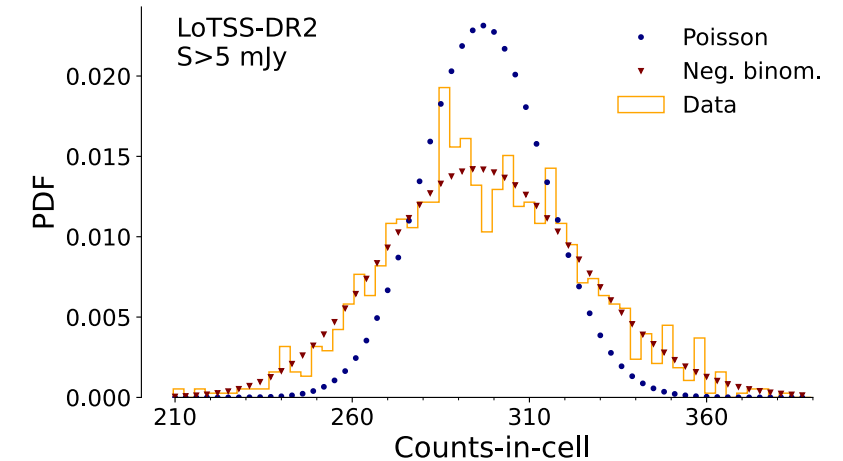
Negative binomial distribution

Poisson distributed physical objects

Model: $N = \sum_{j=1}^O C_j$

Count of radio sources in cell

Number components of object j , distributed logarithmic with p



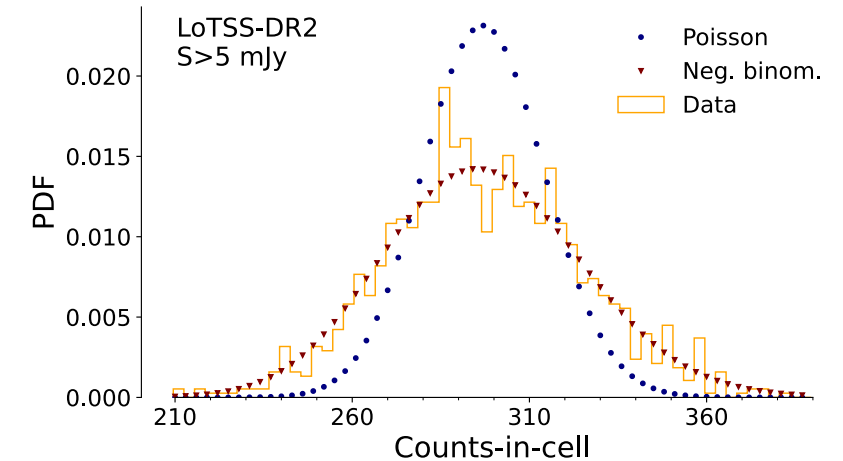
Negative binomial distribution

Poisson distributed physical objects

Model: $N = \sum_{j=1}^O C_j$

Count of radio sources in cell

Number components of object j , distributed logarithmic with p



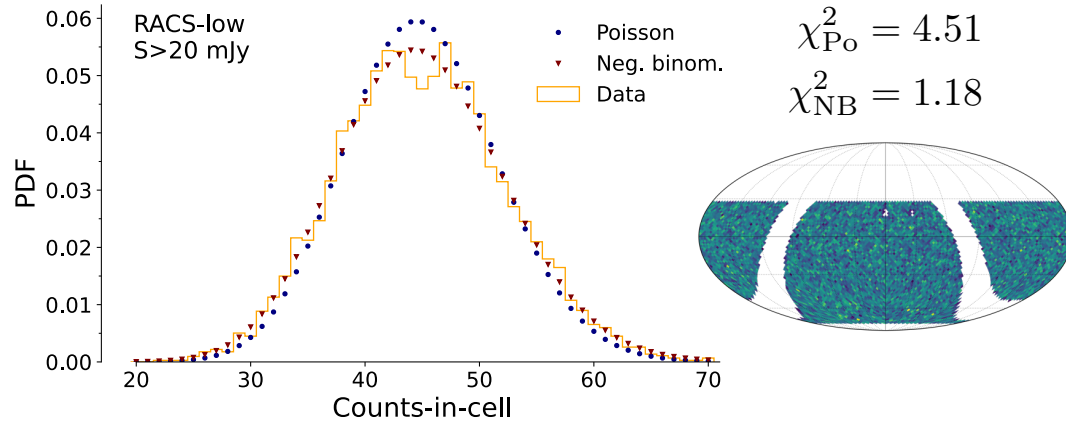
$$P_{\text{NB}}(N) = \binom{N + r - 1}{N} p^N (1 - p)^r$$

$$p = 1 - \frac{\mathbb{E}[\text{Data}]}{\text{Var}[\text{Data}]}, \quad r = \frac{\mathbb{E}[\text{Data}]^2}{\text{Var}[\text{Data}] - \mathbb{E}[\text{Data}]}$$

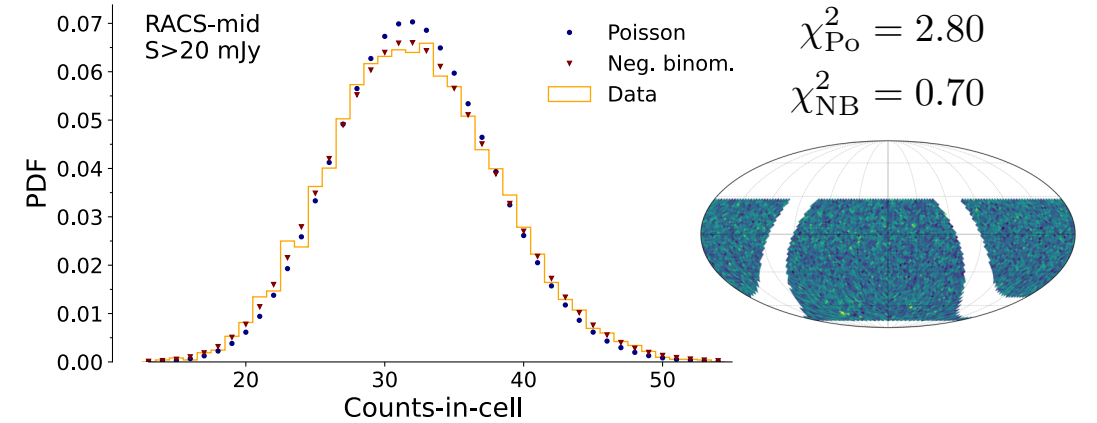
$p \rightarrow 0$
 $r \rightarrow \infty$ Poissonian limit, $0 < p < 1$: Clustering

Data distribution

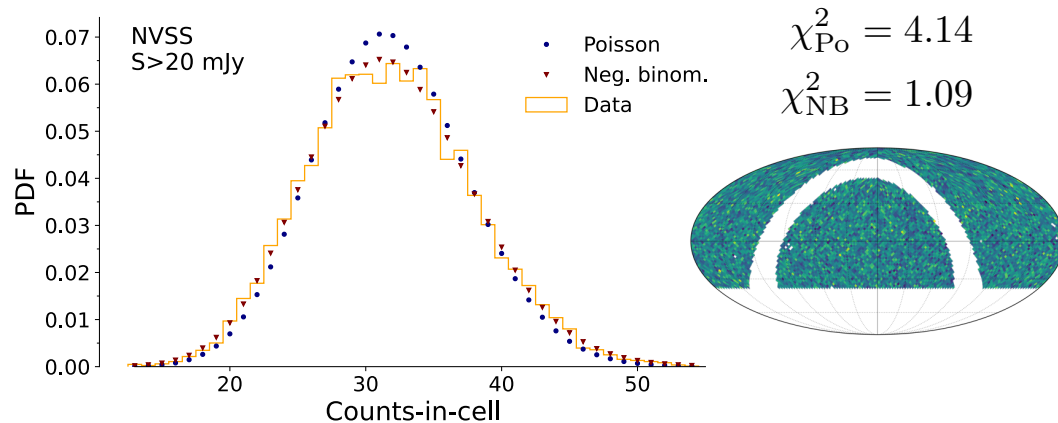
RACS-low ($S_{\min} = 20$ mJy, 888 MHz)



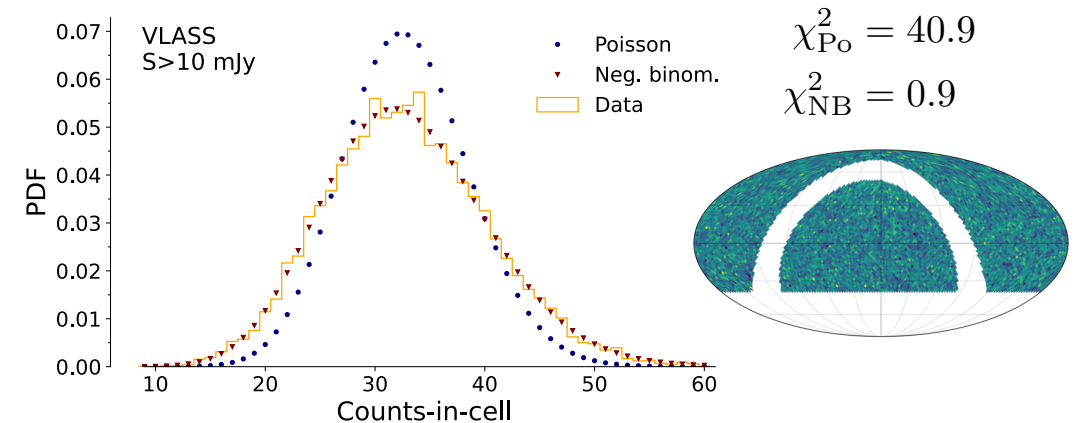
RACS-mid ($S_{\min} = 20$ mJy, 1368 MHz)



NVSS ($S_{\min} = 20$ mJy, 1400 MHz)



VCLASS ($S_{\min} = 10$ mJy, 3000 MHz)



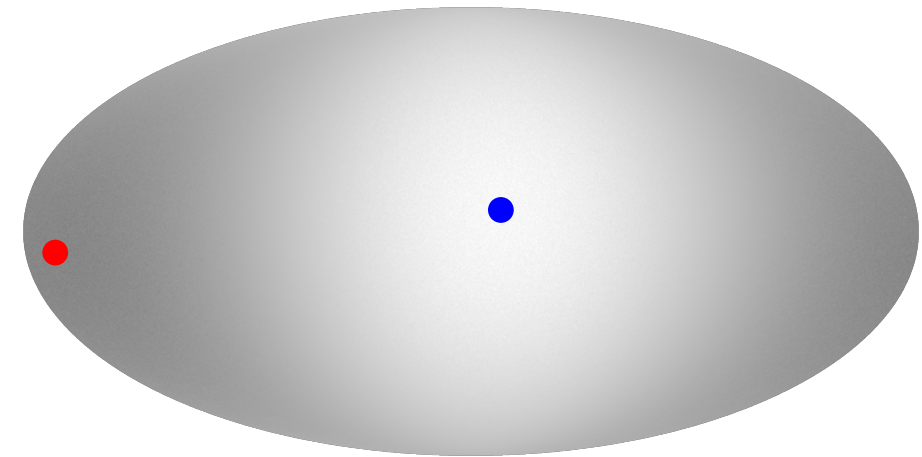
Estimator for radio source counts

- Likelihood for the negative binomial distr. with dipole given by:

$$L(n|\mathbf{d}) = \sum_i \binom{n_i + r_i - 1}{n_i} (1 - p)^{n_i} p^{r_i}$$

Dipole affects mean count as a function of direction

$r_i = r(1 + d \cos \theta_i)$



Estimator for radio source counts

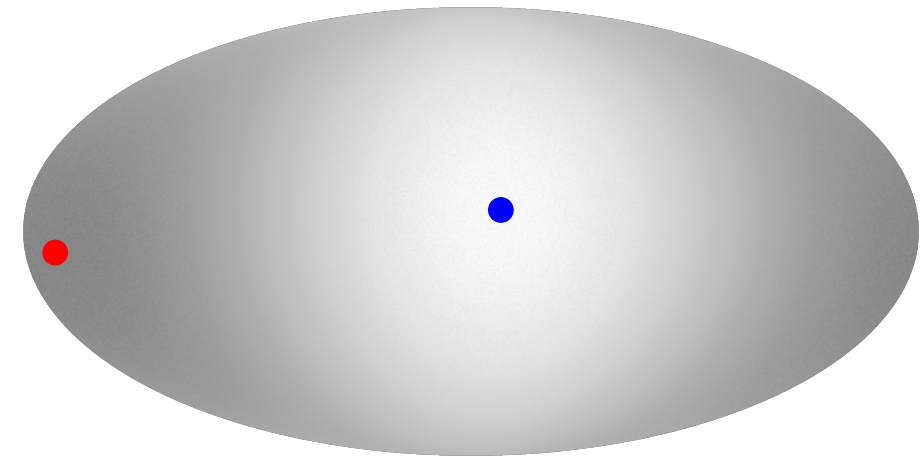
- Likelihood for the negative binomial distr. with dipole given by:

$$L(n|\mathbf{d}) = \sum_i \binom{n_i + r_i - 1}{n_i} (1 - p)^{n_i} p^{r_i}$$

Dipole affects mean count as a function of direction

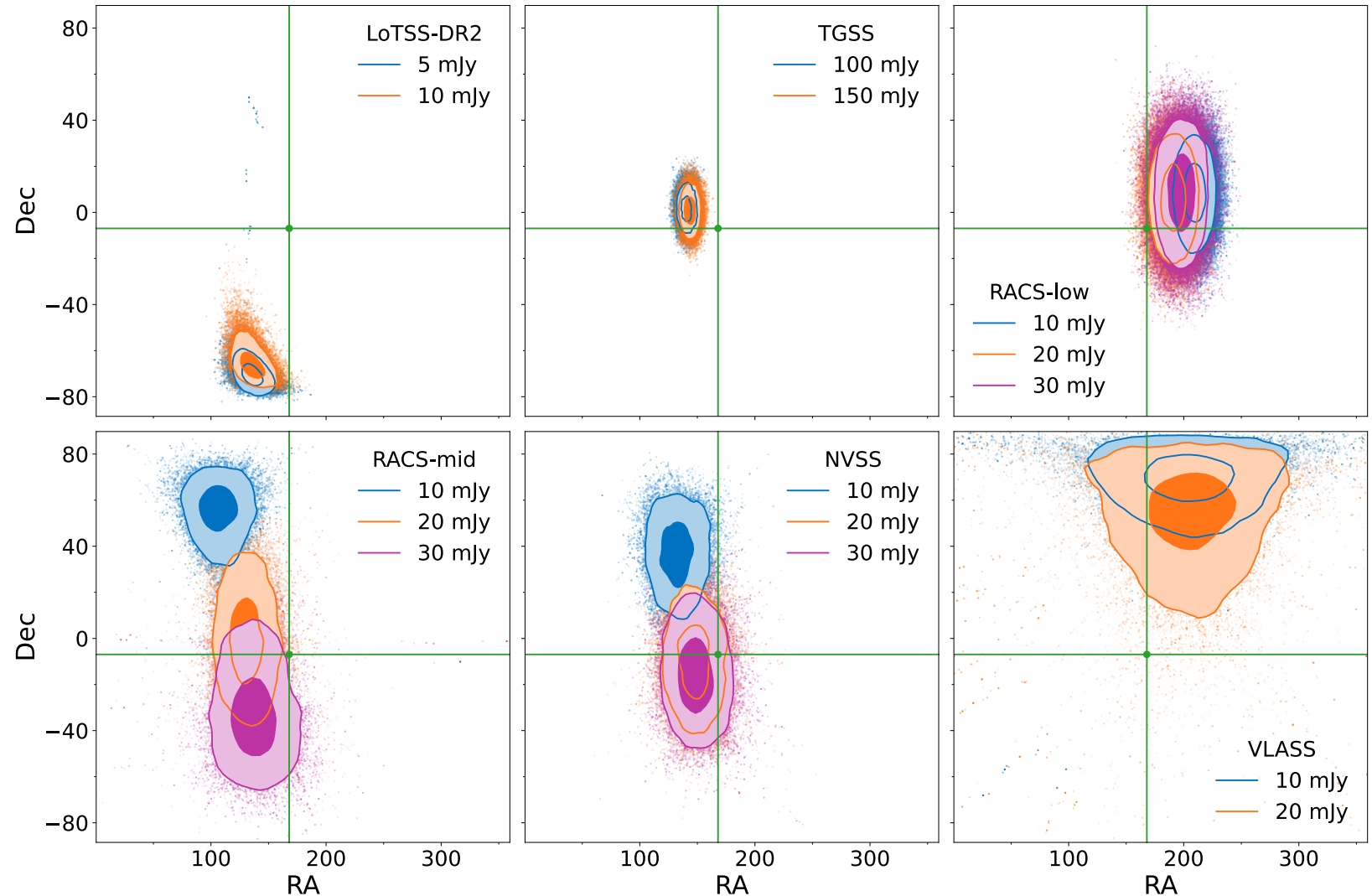
$r_i = r(1 + d \cos \theta_i)$

- Minimise the negative log-likelihood with Bilby [1,2]
- Multi-survey estimation:
 - Add log-likelihoods to obtain a combined estimate
 - +Assume: Same underlying dipole in all surveys



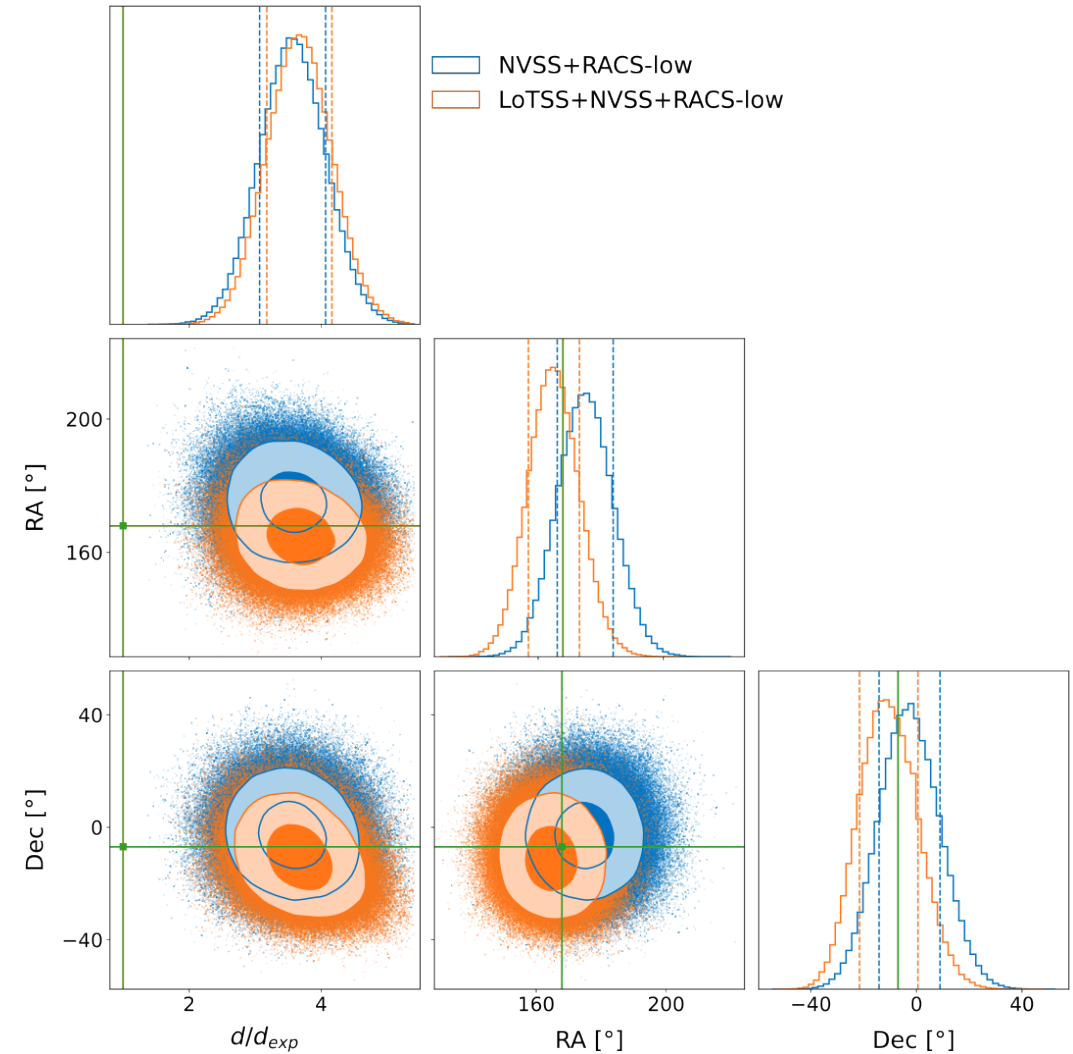
Radio Dipole

- LoTSS-DR2 alone:
too small sky coverage
- TGSS:
abnormal amplitude
- RACS-mid:
inconsistent
- VLASS:
problematic issues



Joint estimate

- Combine
 - LoTSS-DR2
 - RACS-low
 - NVSSto get coverage + sensitivity
- A factor 3.67 ± 0.49 higher than CMB, direction well aligned
- Through the addition of LoTSS-DR2: 5.4σ discrepancy in amplitude to CMB



Conclusion, future prospects

- Joint estimate raises significant tension with CMB, consistent with previous measurements
- Future large area sky surveys will help
- Wide-field spectroscopic follow ups:
WEAVE-LOFAR -> Removing low- z /local sources